

## B.1 Examples and Exercises

### B.1.1 - Probability Functions

*Slide 5/27:*

Express the probability that a (30) dies between ages 40 and 45 using the cumulative distribution function.

*Slide 7/27:*

Express the probability that a (30) dies between ages 40 and 45 using the survival function.

*Slide 9/27:*

Write the probability that a 50 year old dies between ages 51 and 53 using the curtate future lifetime random variable.

*Slide 10/27 (Exercise):*

You are given a survival function  $S_0(x) = 1 - 0.01x$  for  $0 \leq x \leq 100$ .

Determine the median future lifetime of a life aged 10.

### B.1.2 - Actuarial Notation for Probabilities

*Slide 18/27 (Exercise):*

You are given  ${}_1|q_{x+1} = 0.095$ ,  ${}_2|q_{x+1} = 0.171$  and  $q_{x+3} = 0.200$ . Calculate  $q_{x+1} + q_{x+2}$ .

### B.1.3 - Life Tables

*Slide 25/27 (Exercise 1):*

You are given  ${}_1|q_{x+1} = 0.095$ ,  ${}_2|q_{x+1} = 0.171$  and  $q_{x+3} = 0.200$ . Calculate  $q_{x+1} + q_{x+2}$ . (Hint: build a table)

*Slide 26/27 (Exercise 2):*

You are given the following:

- A. The probability that a person age 20 will survive 30 years is 0.7.
- B. The probability that a person age 45 will die within 5 years and that another person age 40 will survive 5 years is 0.0475.
- C. The probability that a person age 20 will survive 20 years and that another person age 40 will die within 5 years is 0.04.

Calculate the probability that a person age 20 will survive 25 years.